## Complexity Theory

## Due date: July 10, 2012 before class!

## Problem 1 (10 Points)

Show that
(i) RP and BPP are closed under $\preceq_{m}^{p}$,
(ii) $\mathbf{R P}$ and $\mathbf{B P P}$ are closed under union and intersection.

## Problem 2 (10 Points)

Show that, if $\mathcal{N P} \subseteq \mathbf{B P P}$, then $\mathbf{R P}=\mathcal{N} \mathcal{P}$.

## Problem 3 (10 Points)

Show that RP does not change if we replace in the definition $\geq 2 / 3$ by $\geq n^{-k}$ or by $1-2^{-n^{k}}$.

## Problem 4 (10 Points)

Prove that $\mathbf{Z P P}=\mathbf{R P} \cap \mathrm{co}-\mathbf{R P}$.

