WS 2015/16 Worksheet 3 2.11.2015

Fundamental Algorithms 3

Exercise 1

Consider a partitioning algorithm that, in the worst case, will partition an array of *m* elements into two partitions of size $\lfloor \epsilon m \rfloor$ and $\lceil (1 - \epsilon)m \rceil$, where ϵ is fixed, and $0 < \epsilon < 1$. Show that a quicksort algorithm based on this partitioning has a worst-case complexity of $O(n \log n)$.

Hint or solution: solve the recurrence by guessing the solution and finding the involved constants.

K-Exercise 2 (An Iterative MergeSort)

The following iterative implementation of the MergeSort algorithm is proposed:

The procedure MergeIP is equivalent to the procedure **Merge** discussed in the lecture, but can work directly on the array A (i.e., merges two adjacent subarrays of A).

- a) Describe shortly and in plain words, how ItMergeSort compares to the recursive MergeSort implementation discussed in the lecture. For that purpose, draw a diagram that illustrates the sorting of an array A[0..7] for ItMergeSort.
- **b**) Formulate a loop invariant for the L-loop of the algorithm, and prove its correctness.